### माध्यमिक शिक्षा परीक्षा

# (Secondary Education Examinations - SEE) अनिवार्य गणित

समय : 3:00 घण्टा पूर्णाङ्ग : 100

सबै प्रश्नहरूहलगर्नुहोस् । Attempt all the Questions.

# समूह 'क' (Group 'A') $[3 \times 2 = 6]$

1. (a) मुल्यअभिवृद्धि करको परिभाषा लेख्नुहोस् ।

Write down the definition of Value Added Tax (VAT).

(b). कुनै त्रिभुजका तिन ओटा भुजाहरू क्रमश : a, b र c छन् भने सो त्रिभुजको अर्धपरिमिति कित हन्छ, लेख्नुहोस् ।

If three sides of a triangle are a,b and c respectively, what is the semi perimeter of the triangle? Write it.

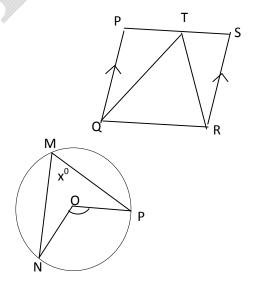
2. (a) सरल गर्नुहोस् (Simplify):

$$x^{a-b}x x^{b-a}$$

- (b). वर्गीकृत तथ्याङ्कमातल्लो चतुर्थांशको मान  $(Q_1)$  पत्तालगाउने सूत्र लेख्नुहोस् । Write the formula to find the value of lower quartile (Q1) of a continuous data.
- 3. (a) दिइएको चित्रमा समानान्तर चर्तुभुज PQRS र

 $\Delta QTR$  को क्षेत्रफल बीच के सम्बन्ध हुन्छ, लेख्नुहोस्। In the given figure, what is the relation between the area of the parallelogram PQRS and the  $\Delta QTR$ ? Write it.

(b). सँगैका चित्रमा 0 वृत्तको केन्द्रबिन्दु हो । यदि  $\angle NMP = x^0$  भए  $\angle NOP$  को मान पत्ता लगाउनुहोस् । In the adjoining figure, O is the center of a circle. If  $\angle NMP = x^0$ , find the value of  $\angle NOP$ .



## समूह 'ख' (Group 'B') [7 x (2+2) +3 x (2+2+2) =34]

4. (a) एउटा वस्तुको 13% मूल्यअभिवृद्धि करसिंहतको मूल्य रु. 5763 छ भने मुल्यअभिवृद्धि कर रकम कित होला ? पत्ता लगाउनुहोस्।

The price of an object with 13% value added tax is Rs. 5763. What will be the value added tax amount? Find it.

- (b). एउटा मोटरसाइकलको हालको मूल्य रु.2,25,000 छ। यदि सो मुल्यमा प्रतिवर्ष 8% का दरले बार्षिक हास हुन्छ भने, कित वर्षपछि मोटरसाइकलको मुल्य रु. 1,75,204.80 होला ? पत्ता लगाउनुहोस्। The present price of a motorcycle is Rs. 2,25,000. If its price is depreciated per year by 8%, after how many years will be the price of the motorcycle be Rs. 1,75,204.80? Find it.
- 5. (a) आधार भुजाको लम्बाइ 10 मिटर भएको एउटा समद्विबाह त्रिभुजाकार जग्गाको क्षेत्रफल 60 वर्ग मिटर भए सो जग्गाको बाँकी भुजाहरूको नाप पत्ता लगाउनुहोस्।

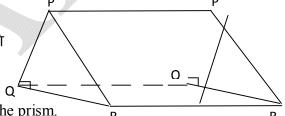
The area of anisosceles triangular land whose base side length 10 meter is 60 square meter. Find the measure of its remaining sides.

(b). आधारको व्यास 14 से.मि. भएको एउटा बेलनाको आयतन 2156 घन से.मि. छ भने सो बेलनाको उचाइ पत्ता लगाउन्होस् ।

The volume of a cylinder with diameter of its base 14 cm is 2156 cubic cm. Find the height of the cylinder.

(c). दिइएको ठोस त्रिभुजाकार प्रिज्ममा यदि  $PQ \perp QR$ , PQ = 8 से.मि., QR = 6 से.मि. र  $RR^1 = 15$  से.मि. छन् भने सो प्रिज्मको छड्के सतहको क्षेत्रफल पत्ता लगाउनुहोस् ।

In the given solid triangular prism, if  $PQ \perp QR$ , PQ = 8cm, Q = 6cm and  $RR^1 = 15$  cm, find the lateral surface area of the prism.



6. (a) सरल गर्नुहोस (Simplify):

$$2\sqrt{98} - 8\sqrt{32} + 3\sqrt{72}$$

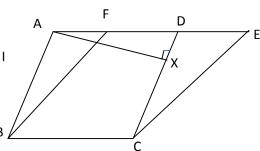
(b). हलगर्न्होस् (Solve):

$$9-\sqrt{x-4}=5$$

- 7. (a)मान निकाल्नुहोस् (Evaluate) :  $\frac{3\times 4^{x} + 4^{x-1}}{13\times 4^{x}}$ 
  - (b). कुनै घनात्मक सङ्ख्याको वर्गमा 5 जोडदा योगफल 69 हुन्छ भने उक्त सङ्ख्या पत्ता लगाउनुहोस्। If 5 is added to the square of a positive number, the sum is 69. Find the number.
  - (c). सरल गर्नुहोस् (Simplify):

$$\frac{1}{(x-y)} - \frac{1}{(x+y)} + \frac{2x}{x^2 - y^2}$$

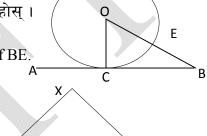
8. (a) दिइएको चित्रमा BC// AE, BA//CD, BF// CE /AX\_CD छन्।



यदि AB = 12 से.मि. र चर्तुभुज BCEF को क्षेत्रफल 84 वर्ग से.मि. छभने AX को लम्बाइपत्तालगाउनुहोस्। In the given figure, BC// AE, BA//CD, BF// CE and  $AX \perp CD$ . If AB = 12 cm and area of the quadrilateral BCEF = 84 sq. cm., find the length of AX.

(b). दिइएको चित्रमाOवृत्तको केन्द्रबिन्दु र MNPQ एउटा चकीय चतुर्भुजहो । यदि NR= NP /  $\angle$ PNR =  $50^{0}$  भए  $\angle$ NMQ को नाप पत्ता लगाउनुहोस् । In the given figure, O is the centre of the circle and MNPQ is a cyclic quadrilateral. If NR = NP and  $\angle$ PNR =  $50^{0}$ , find the size of  $\angle$ NMQ.

(c). दिइएको चित्रमा O वृत्तको केन्द्रिबन्दु र AB स्पर्श रेखा हो। यदि OC = 5 से.मि. र BC = 12 से.मि. भए BE को नाप पत्ता लगाउनुहोस्। In the given figure, O is the center of the circle and AB is a tangent line. If OC= 5 cm and BC = 12 cm, find the measure of BE.



0

9. (a) दिइएको त्रिभुज XYZ मा XY = 8 से.मि., YZ = 12 से.मि.
 र ΔXYZ को क्षेत्रफल 24 वर्ग से.मि. छन् भने ΔXYZ को नाप पत्ता लगाउनुहोस्।

In the given triangle XYZ, XY = 8 cm, YZ = 12 cm and area of  $\Delta XYZ$  is 24 sq. cm., find the size of  $\Delta XYZ$ .

b). एउटा वर्गीकृत तथ्याङ्कमा, यदि पदहरूको सङ्ख्या (N) = 9b+5,  $\sum fm = 350$  र मध्यक  $(\overline{X}) = 7$  भए N को मान पत्ता लगाउन्होस् ।

In a grouped data, if the number of terms (N) =9b+5, $\sum$ fm = 350 and Mean ( $\overline{X}$ )= 7, find the value of N.

10. (a) एउटा डाइसलाई उफार्दा 3 ले भाग जाने सङ्ख्या अथवा वर्ग सङ्ख्या आउने सम्भाव्यता कित हुन्छ ? पत्ता लगाउनुहोस्।

Find the probability of getting a number divisible by 3 or a square number when a fair dice is thrown.

(b). 10 ओटा राता र 6 ओटा काला उत्रै र उस्तै बलहरू भएको एउटा भोलाबाट एकपछि अर्को गरी पुन: नराखी 2 ओटा बलहरू क्रमशः भिक्दा आउने सबै परिमाणका सम्भाव्यतालाई वृक्षचित्रमा देखाउनुहोस्। From a bag containing 10 red and 6 black balls of the same shape and size, two balls are taken randomly in succession without replacement. Show the probabilities of all outcomes in a tree diagram.

## समूह 'ग' (Group' C') [10x4=40]

- 11. 180 जना विद्यार्थीहरूको समूहमा सर्वेक्षण गर्दा 50 जनाले क्रिकेट खेलमात्र मन पराउँछु भने, 30 जनाले बास्केट बल खेलमात्र मन पराउँछु भने र 50 जनाले दुवै खेल मन पराउँदैनौं भन्यो भने, In a survey of a group of 180 students, 50 students say to like cricket game only, 30 students say to like basketball game only and 50 students say do not like both games.
  - i) माथिको भनाइलाई भेन चित्रमा प्रस्तुत गर्नुहोस्। Represent the above information in a Venn diagram.
  - ii) क्रिकेट खेल मन पराउने र बासकेट बल खेल मन पराउने विद्यार्थीहरूको अनुपात पत्ता लगाउनुहोस्।

Find the ratio of the students who like cricket game and basketball game.

12. मनिषले रु. 2,00,000 मा केही अमेरिकी डलर किने। तर चार दिनपछि अमेरिकी डलरको तुलनामा नेपाली मुद्रा 5% ले अवमूल्यन भयो। नेपाली मुद्रा अवमूल्यन भएको दिन मनिषले फेरी नेपाली रुपियाँ साट्दा उसलाई कित नाफा वा नोक्सान हुन्छ ? पत्ता लगाउनुहोस्। (\$1 = NRs. 104.28)

Manish bought some American dollar for Rs. 2,00,000. But after four days, the Nepalese currency was devaluated in the comparison of American dollar by 5%. Again Manish exchanged the Nepali currency by giving American dollar in the day of devaluation of Nepalese currency. How much does he gain or loss? Find it.-\$1 = NRs.104.28\_

13. छड्के उचाइ 10 से.मी. र ठाडो उचाइ 8 से.मी. भएको एउटा वर्गाकार आधार भएको पिरामिडको परा सतहको क्षेत्रफल पत्ता लगाउनहोस ।

Find the total surface area of a square based pyramid having the slant height 10 cm and vertical height 8cm.

14. म.स.निकाल्नुहोस् (Find the H.C.F. of):

 $a^3+1+2a^2+2a$ ,  $a^3-1$  and  $a^4+a^2+1$ 

15. सरल गर्नुहोस् (Simplify):

$$\frac{x}{(x-y)(x-z)} + \frac{y}{(y-z)(y-x)} + \frac{x}{(z-x)(z-y)}$$

16. एउटै आधार MN र उही समानान्तर रेखाहरु MN र PQ बीचमा बनेका त्रिभुज PMN र समानान्तर चतुर्भुज RMNQ हुन् भने सिद्ध गर्नुहोस् :

 $\Delta$  PMN को क्षेत्रफल =  $\frac{1}{2}$   $\square$  RMNQ को क्षेत्रफल।

A triangle PMN and a parallelogram RMNQ are constructed on the same base MN and between the same parallel lines MN and PQ. Prove that: area of  $\Delta PMN = \frac{1}{2}$  arealof RMNQ.

17. PQ = 5 से.मी, QR = 5.6 से.मी, Rs = 5.4 से.मी. SP = 6.8 से.मी र  $\angle PQR = 750$  भएको एउटा चतुर्भुज PQRS को रचना गरी उक्त चतुर्भुजको क्षेत्रफलसँग बराबर हुने गरी एउटा त्रिभुज PSM को रचना गर्नुहोस् ।

- Construct a quadrilateral PQRS in which PQ=5cm, QR=5.6cm, Rs=5.4cm, SP=6.8cm, and  $\angle PQR=75^{\circ}$ . Then construct a triangle PSM equal in area to the quadrilateral PQRS.
- 18 .वृत्त ABC को एउटै चाप AC मा आधारित केन्द्रीयकोण APC र परिधिकोण ABC बीचको सम्बन्ध प्रयोगद्वारा परीक्षण गरी पत्ता लगाउनुहोस् । कम्तीमा 3 से.मी. अर्धव्यास भएका दुईवटा वृत्तहरु आवश्यक छन् ।)
  - Explore experimentally the relation between the central angle APC and the circumference angle ABC standing on the same arc AC of a circle ABC. (Two circles of radii not less than 3cm are necessary.)
- 19. 1.5 मिटर अग्लो मानिसले 41.5 मिटर अग्लो एउटा रुखको ठीक अगाडि उभिएर रुखको टुप्पोमा हेर्दा आँखमा 45<sup>0</sup> को कोण बनेछ भने, उक्त रुख र मानिस बीचको दूरी पत्ता लगाउनुहोस्। A 1.5 meters tall person is standing in front of 41.5 meters high tree. When observing the top of the tree an angle of 450 is formed with the eyes. Find the distance between the tree and the person.
- 20. यदि तल दिएको आँकडाको मध्यिका 19 भए P को मान पत्ता लगाउनुहोस्। If the median of the following given data is 19, find the value of P.

उमेर वर्षमा (Age in Year)	6-12	12-18	18-24	24-30	30-36	36-42
विद्यार्थी संख्या (Number Of Students)	4	10	P	4	3	3

# समूह 'घ' (Group D) [4x5 =20]

- 21. एउटा बैंकले खाता A मा10% प्रति वर्ष अर्धवार्षिक चकीय व्याजदर र खाता B मा 12% प्रति वर्ष वार्षिक चकीय व्याजदर कायम गरेको छ। यदि तपाई 2 वर्षका लागि रु. 25,000 सो बैकमा जम्मा गर्दै हुनुहुन्छ भने कुन खातामा जम्मा गर्नु हुन्छ र किन ?गणनागरी कारणसहित उल्लेख गर्नुहोस्। A bank has fixed the rate of interest 10% per annum semiannually compound interest in account A and 12% per annum annually compound interest in account B. If you are going to deposit Rs. 25,000 for 2 years in the same bank, in which account will you deposit and why? Give your reason with calculation.
- 22. एक जना मानिसले आफ्नो घरको प्रयोजनको लागि 1.05 मिटर अर्धव्यास र 3.5 मिटर उचाइ भएको एउटा वृताकार आधार भएको पानी ट्याङ्की पसलबाट किनेर ल्याउनु भयो। यदि उक्त ट्याङ्कीको माथिल्लो भाग अर्धगोलाकार छ भने सो ट्याङ्कीमा कित लिटर पानी अटाउँछ होला ? पत्ता लगाउनुहोस्।
- A person bought a water tank of circular base having the radius 1.05 meter and height 3.5 meter for the use of own house from the shop. If the upper part of the tank is semi spherical, how many liters of water will be contained in the tank? Find it.
- 23. यदि तिन वर्ष अघि बाबु र छोराको उमेरको योगफल 48 बर्ष थियो। अबको 3 बर्ष पछि बाबु र छोराको उमेरको अनुपात 3:1 हुन्छ भने छोरा भन्दा बाबु कित वर्षले जेठो हुनुहुन्छ ? पत्ता लगाउनुहोसु।

Three years ago, the sum of the ages of the father and son was 48 years. After three years the ratio of the ages of the father and son will be 3: 1, then how much old is the father from his son? Find it.

24. दिइएको चित्रमा ABCD एउटा चकीय चतुर्भुजहो । भुजा CD लाई लम्बयाएर E सम्म पुऱ्याइएको छ । यदि AD ले ΔBDE लाई आधा गरेको छ भने ΔABC एउटा समद्विवाहु त्रिभुज हो भनी प्रमाणित गर्नुहोस् ।
In the given figure, ABCD is a cyclic quadrilateral. The side CD is produced to E. If AD bisects ΔBDE, prove that ΔABC is an isosceles triangle.



# **Marking Scheme**

#### Group 'A' $[3 \times (1+1) = 6]$

- 1. a. Correct definition of VAT.....(1)
  - b. Semi perimeter of a triangle =  $\frac{a+b+c}{2}$ .....(1)
- 2. a.  $x^{a-b+b-a} = x^0 = 1$ ....(1)
  - b. Value of  $Q_1 = L + \frac{\frac{N}{4} c.f.}{f} \times i...$  (1)
- 3. a. Area of  $\triangle QTR = \frac{1}{2} \text{ area } d \overline{P}$  PQRS.....(1)
  - b.  $\angle NOP = 2x^0$ ....(1)

#### Group 'B' [4x (2+2) + 3x (2+2+2) = 34]

4. a. i. Let the price of the object with VAT be Rs. x.

Then, 
$$\frac{113x}{100} = 5763$$

$$\therefore x = \text{Rs. } 5100....(1)$$

$$= Rs. 663....(1)$$

b. i. 
$$175204.80 = 225000 \left(1 - \frac{8}{100}\right)^{T}$$
 .....(1)

ii. 
$$T = 3$$
 years....(1)

5. a. i. 
$$\frac{1}{2} \times 10 \times \frac{\sqrt{4a^2 - 100}}{2} = 60$$
 .....(1)

b. i. 
$$r = 7cm$$

$$2156 = \pi (7)^2 \times h....(1)$$

c. i. PR = 
$$\sqrt{(8)^2 - (6)^2}$$
 = 10 cm....(1)

ii. Area of the lateral surface of the prism = (8+6+10) cm  $\times$  15 cm

6. a. i. 
$$14\sqrt{12} - 32\sqrt{2} + 18\sqrt{2}$$
 .....(1)

b. i. 
$$16 = x - 4$$
....(1)

ii. 
$$x = 20$$
....(1)

7. a. i. 
$$\frac{4^x(3+1/4)}{13\times 4^x}$$
 ......(1)

ii. 
$$\frac{1}{4}$$
.....(1)

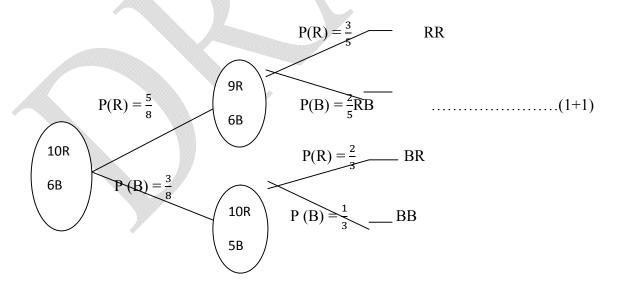
b. i. Let a positive number be x.

$$x^2 + 5 = 69$$
 .....(1)

ii. 
$$x = 8$$
 .....(1)

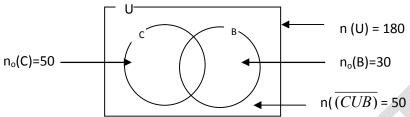
b) i) let R and B denote red balls and black balls respectively.

ii)p(3 or s)= $\frac{2}{6} + \frac{2}{6} = \frac{2}{3}$ ....(1)



#### Group - 'C'

11. Let C and B represent sets of students who like cricket game and basketball game respectively, x be number of students who like both and U be the universal set.



- I. Representation of the information Venn-diagram 1 II.  $n(C \cup B) = n(U) - n(CUB) = 180 - 50 = 130$ 1 III.  $n(C \cap B) = x=n(CB)-n(C)-n(B)=130-50-30=50$ 1 IV. n(C)=50+50=100 and n(B)=30+50=80n(C) : n(B) = 100 : 80 = 5 : 41 12. i) Rs 104.28= \$1 Therefore Rs 200000= \$1917.91 1 ii)1 = Rs 104.28 + 5% of Rs 104.28 = Rs 109.49iii)\$1917.91= Rs 109.49\*1917.91 = Rs 209991.961 iv) manish makes profit profit= Rs 9991.96 1
- 13. i) slant height (l)=10 cm, vertical height(h)=8 cm.

Let the length of the side of the base of the square based pyramid be a cm. Then

$$10^2 = 8^2 + (a/2)^2 \dots (1)$$

- ii) a = 12cm .....(1)
- iii) T.S.A of the pyramid=  $a^2 + 2al$

$$=12^2 + 2 * 12 * 10$$
 .....(1)

iv.) = 
$$384 \text{ sq.cm}$$
 (1).

14. i.) 
$$1^{st} \exp = a^3 + 1 = (a+1)(a^2-a+1)$$
....(1)

ii.) 
$$2^{nd} \exp = a^3 - 1 = (a-1)(a^2 + a + 1)...(1)$$

iii.) 
$$3^{rd}$$
 exp. =  $a^4 + a^2 + 1 = (a^2 + a + 1) (a^2 - a + 1)$ ....(1)

iv.) L. C. M. = 
$$(a+1)(a-1)(a^2+a+1)(a^2-a+1)$$
....(1)

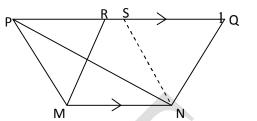
15. I. 
$$-\frac{x}{(x-y)(z-x)} - \frac{y}{(y-z)(x-y)} - \frac{z}{(z-x)(y-z)}$$

II. 
$$-\frac{x(y-z)+y(z-x)+z(x-y)}{(x-y)(z-x)(y-z)}$$

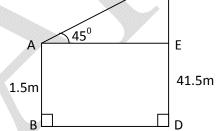
III. 
$$-\frac{x(y-z)+zx-xy}{(x-y)(y-z)(z-x)}$$

1

- 16. i. Correct figure, Given and To prove.
  - ii. Construction: Draw NS//MP
  - iii. Area of MNS = area of RNNQ
  - iv. Area of  $\triangle$  PMN =  $\frac{1}{2}$  area of  $\triangle$ MNQ



- - II. For correct construction of quadrilateral PQRS ...... 1
  - III. For construction of a line RM parallel to a diagonal SQ. ...... 1
- - III. Correct conclusion ...... 1
- 19. I. Appropriate figure with correct description .......... 1
- III. In right angled  $\triangle AEC$ ,



- 20. I. Frequency table

/ - 1 /		
Age in years	No. of students (f)	C.F.
6-12	4	4
12-18	10	14
18-24	р	14+p
24-30	4	18+p
30-36	3	21+p
36-42	3	24+p

- II. Here, Median (Md) = 19, so median class = 18 24 ...... 1
- III. Median(md) =  $L + \frac{\frac{N}{2} c.f.}{f} \times i$

### Group 'D' (4×5=20)

21.	Interest in account A			
21.				
	(i) $CI_1 = P[(1 + \frac{10}{200})^{2X^2} - 1] = \dots$	1		
	= Rs. 5387.65	1		
	Interest in account B			
	(ii) $CI_2 = P[(1 + \frac{12}{100})^2 - 1] = \dots$			
	= Rs. 6360	1		
	(iii) Here it is more convinient to deposit Rs.25000 in account B. Because the interest in account B is more than the interest in account A by,			
	Rs. 6360 - Rs. 5387.65 = Rs. 972.35	1		
22.	(i) Here, radius of base (r) = 1.05 m			
22.	Total height of the tank $(H) = 3.5 \text{ m}$			
		1		
	Radius of the hemi-spherical part of the tank = $r = 1.05m$ (fig)	1		
	Hence the height of the cylindrical part of the tank (h) = $3.5\text{m}$ - $1.05\text{m}$ = $3.45\text{m}$			
	(ii) Volume of the cylindrical part = $\pi r^2 h =$			
	$= 11.955 \text{ m}^3$	1		
	(iii) Volume of hemispherical part = $2/3 \pi r^3 = \dots$			
	$= 2.427 \text{m}^3$	1		
	(iv) Total volume of water $tank = 11.955m^3 + 2.427m^3$			
	$= 14.382 \text{m}^3$	1		
	(v) Volume of water = volume of the tank = $14.382$ m <sup>3</sup>			
	= 14.382 X 1000 l			
	= 14 382 liters	1		
23.	(i) Let present ages of the father and his son be x years and y years respectively.			
	Then, three years ago, $(x-3) + (y-3) = 48$			
	or, $x + y = 54$			
	(ii) Again, after three years, $(x + 3) : (y+3) = 3:1$	1		
	or, $x - 3y = 6$			
	(iii) solving the above equation we get,	1		
	y = 12			
L				

	(iv) Again putting the value of y, in any of the above equation we get,	
	x = 42	1
	(v) Hence the differnce between their ages = $42-12=30$ ,	
	Hence the father is 30 years older than his son.	1
24.	(i) ≰ADE = ≰ADBwith reason	1
	(ii) ≰ADE = ≰ABC with reason	1
	(iii) ≰ADB= ≰ACB with reason	1
	(iv) ≰ABC = ≰ACBwith reason	1
	(v) Δ ABC is an isoscelaces triangle, with reason	1

